

Title

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Abstract. By using the computer program “Discoverer”, we give theorems about anticevian corner products.

Keywords. anticevian corner product, triangle geometry, remarkable point, computer-discovered mathematics, Euclidean geometry, Discoverer.

Mathematics Subject Classification (2010). 51-04, 68T01, 68T99.

1. INTRODUCTION

$ABC \ \mathcal{ABC} \ \text{ABC} \ \text{ABC} \ \text{ABC} \ \mathfrak{ABC} \ \overrightarrow{PQ}$

2. PRELIMINARIES

2.1. Barycentric Coordinates.

Definition 2.1. *Definition.*

Example 2.1. *Example.*

Lemma 2.1. *Lemma.*

Theorem 2.1. *Theorem.*

Proof. The proof. □

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Corollary 2.1. *Corollary.*

Remark. *Remark.*

Theorem 2.2 (Pythagorean theorem). *Theorem.*

Theorem 2.3 (Gibert's theorem). *Theorem.*

$$(1) \quad |PQ|^2 = -a^2vw - b^2wu - c^2uv$$

where $u = u_1 - u_2, v = v_1 - v_2$ and $w = w_1 - w_2$.

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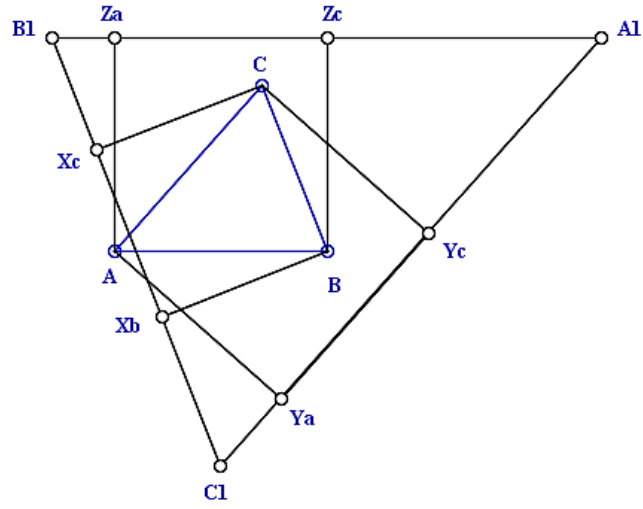


FIGURE 1. PNG figure

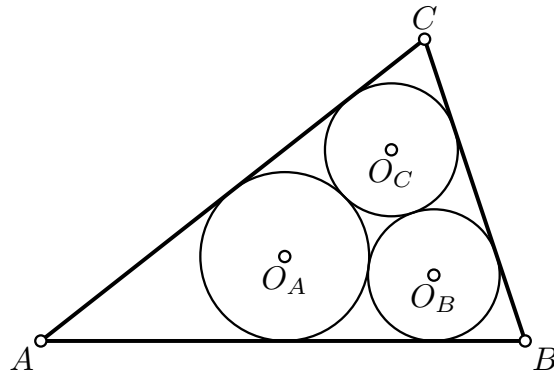


FIGURE 2. EPS figure

Determinant:

$$(2) \quad \begin{vmatrix} u_1 & v_1 & w_1 \\ u_2 & v_2 & w_2 \\ x & y & z \end{vmatrix} = 0.$$

Matrix:

$$(3) \quad A = \begin{bmatrix} u_1 & v_1 & w_1 \\ u_2 & v_2 & w_2 \\ x & y & z \end{bmatrix}$$

$$(4) \quad B = \begin{pmatrix} u_1 & v_1 & w_1 \\ u_2 & v_2 & w_2 \\ x & y & z \end{pmatrix}$$

$$\frac{a}{x} + \frac{b}{y} + \frac{c}{z\sqrt{2}} = 0.$$

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